

4. EMPIRICIST CRITERIA

OF COGNITIVE SIGNIFICANCE:

PROBLEMS AND CHANGES

1. THE GENERAL EMPIRICIST CONCEPTION OF COGNITIVE AND EMPIRICAL SIGNIFICANCE

It is a basic principle of contemporary empiricism that a sentence makes a cognitively significant assertion, and thus can be said to be either true or false, if and only if either (1) it is analytic or contradictory—in which case it is said to have purely logical meaning or significance—or else (2) it is capable, at least potentially, of test by experiential evidence—in which case it is said to have empirical meaning or significance. The basic tenet of this principle, and especially of its second part, the so-called testability criterion of empirical meaning (or better: meaningfulness), is not peculiar to empiricism alone: it is characteristic also of contemporary operationalism, and in a sense of pragmatism as well; for the pragmatist maxim that a difference must make a difference to be a difference may well be construed as insisting that a verbal difference between two sentences must make a difference in experiential implications if it is to reflect a difference in meaning.

How this general conception of cognitively significant discourse led to the rejection, as devoid of logical and empirical meaning, of various formulations in speculative metaphysics, and even of certain hypotheses offered within

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empirical science, is too well known to require recounting. I think that the general intent of the empiricist criterion of meaning is basically sound, and that notwithstanding much oversimplification in its use, its critical application has been, on the whole, enlightening and salutary. I feel less confident, however, about the possibility of restating the general idea in the form of precise and general criteria which establish sharp dividing lines (a) between statements of purely logical and statements of empirical significance, and (b) between those sentences which do have cognitive significance and those which do not.

In the present paper, I propose to reconsider these distinctions as conceived in recent empiricism, and to point out some of the difficulties they present. The discussion will concern mainly the second of the two distinctions; in regard to the first, I shall limit myself to a few brief remarks.

2. THE EARLIER TESTABILITY CRITERIA OF MEANING AND THEIR SHORTCOMINGS

Let us note first that any general criterion of cognitive significance will have to meet certain requirements if it is to be at all acceptable. Of these, we note one, which we shall consider here as expressing a necessary, though by no means sufficient, *condition of adequacy* for criteria of cognitive significance.

(A) If under a given criterion of cognitive significance, a sentence *N* is non-significant, then so must be all truth-functional compound sentences in which *N* occurs nonvacuously as a component. For if *N* cannot be significantly assigned a truth value, then it is impossible to assign truth values to the compound sentences containing *N*; hence, they should be qualified as non-significant as well.

We note two corollaries of requirement (A):

(A1) If under a given criterion of cognitive significance, a sentence *S* is non-significant, then so must be its negation, $\sim S$.

(A2) If under a given criterion of cognitive significance, a sentence *N* is non-significant, then so must be any conjunction *N*·*S* and any disjunction *N*∨*S*, no matter whether *S* is significant under the given criterion or not.

We now turn to the initial attempts made in recent empiricism to establish general criteria of cognitive significance. Those attempts were governed by the consideration that a sentence, to make an empirical assertion must be capable of being borne out by, or conflicting with, phenomena which are potentially capable of being directly observed. Sentences describing such potentially observable phenomena—no matter whether the latter do actually occur or not—may be called observation sentences. More specifically, an *observation sentence* might be construed as a sentence—no matter whether true or false—which asserts or denies that a specified object, or group of objects, of macroscopic size

has a particular *observable characteristic*, i.e., a characteristic whose presence or absence can, under favorable circumstances, be ascertained by direct observation.¹

The task of setting up criteria of empirical significance is thus transformed into the problem of characterizing in a precise manner the relationship which obtains between a hypothesis and one or more observation sentences whenever the phenomena described by the latter either confirm or disconfirm the hypothesis in question. The ability of a given sentence to enter into that relationship to some set of observation sentences would then characterize its testability-in-principle, and thus its empirical significance. Let us now briefly examine the major attempts that have been made to obtain criteria of significance in this manner.

One of the earliest criteria is expressed in the so-called *verifiability requirement*. According to it, a sentence is empirically significant if and only if it is not analytic and is capable, at least in principle, of complete verification by observational evidence; i.e., if observational evidence can be described which, if actually obtained, would conclusively establish the truth of the sentence.² With the

1. Observation sentences of this kind belong to what Carnap has called the thing-language, cf., e.g., (1938), pp. 52-53. That they are adequate to formulate the data which serve as the basis for empirical tests is clear in particular for the intensive-testing procedures used in science as well as in large areas of empirical inquiry on the common-sense level. In epistemological discussions, it is frequently assumed that the ultimate evidence for beliefs about empirical matters consists in perceptions and sensations whose description calls for a phenomenistic type of language. The specific problems connected with the phenomenistic approach cannot be discussed here; but it should be mentioned that at any rate all the critical considerations presented in this article in regard to the testability criterion are applicable, *mutatis mutandis*, to the case of a phenomenistic basis as well.

2. Originally, the permissible evidence was meant to be restricted to what is observable by the speaker and perhaps his fellow beings during their life times. Thus construed, the criterion rules out, as cognitively meaningless, all statements about the distant future or the remote past, as has been pointed out, among others, by Ayer (1946), chapter 1; by Pop (1949), chapter 13, esp. pp. 333 ff.; and by Russell (1948), pp. 445-47. This difficulty is avoided, however, if we permit the evidence to consist of any finite set of "logically possible observation data", each of them formulated in an observation sentence. Thus, e.g., the sentence *S*₁: "The tongue of the largest dinosaur in New York's Museum of Natural History was blue or black" is completely verifiable in our sense; for it is a logical consequence of the sentence *S*₂: "The tongue of the largest dinosaur in New York's Museum of Natural History was blue"; and this is an observation sentence, in the sense just indicated.

And if the concept of *verifiability in principle* and the more general concept of *confirmability in principle*, which will be considered later, are construed as referring to *logically possible evidence* as expressed by observation sentences, then it follows similarly that the class of statements which are verifiable, or at least confirmable, in principle include such assertions as that the planet Neptune and the Antarctic Continent existed before they were discovered, and that atomic warfare, if not checked, will lead to the extermination of this planet. The objections which Russell (1948), pp. 445 and 447, raises against the verifiability criterion by reference to those examples do not apply therefore if the criterion is understood in the manner here suggested.

help of the concept of observation sentence, we can restate this requirement as follows: A sentence *S* has empirical meaning if and only if it is possible to indicate a finite set of observation sentences, O_1, O_2, \dots, O_n , such that if these are true, then *S* is necessarily true, too. As stated, however, this condition is satisfied also if *S* is an analytic sentence or if the given observation sentences are logically incompatible with each other. By the following formulation, we rule these cases out and at the same time express the intended criterion more precisely:

(2.1) REQUIREMENT OF COMPLETE VERIFIABILITY IN PRINCIPLE. A sentence has empirical meaning if and only if it is not analytic and follows logically from some finite and logically consistent class of observation sentences.³ These observation sentences need not be true, for what the criterion is to explicate is testability by "potentially observable phenomena," or testability "in principle."

In accordance with the general conception of cognitive significance outlined earlier, a sentence will now be classified as cognitively significant if either it is analytic or contradictory, or it satisfies the verifiability requirement.

This criterion, however, has several serious defects. One of them has been noted by several writers:

a. Let us assume that the properties of being a stork and of being red-legged

3. As has frequently been emphasized in the empiricist literature, the term "verifiability" is to indicate, of course, the conceivability, or better, the logical possibility, of evidence of an observational kind which, if actually encountered, would constitute conclusive evidence for the given sentence; it is not intended to mean the technical possibility of performing the tests needed to obtain such evidence, and even less the possibility of actually finding directly observable phenomena which constitute conclusive evidence for that sentence—which would be tantamount to the actual existence of such evidence and would thus imply the truth of the given sentence. Analogous remarks apply to the terms "falsifiability" and "confirmability". This point has clearly been disregarded in some critical discussions of the verifiability criterion. Thus, e.g., Russell (1948), p. 448 constructs verifiability as the actual existence of a set of conclusively verifying occurrences. This conception, which has never been advocated by any logical empiricist, must naturally turn out to be inadequate since according to it the empirical meaningfulness of a sentence could not be established without gathering empirical evidence, and moreover enough of it to permit a conclusive proof of the sentence in question! It is not surprising, therefore, that his extraordinary interpretation of verifiability leads Russell to the conclusion: "In fact, that a proposition is verifiable is itself not verifiable" (*l.c.*). Actually, under the empiricist interpretation of complete verifiability, any statement asserting the verifiability of some sentence *S* whose text is quoted, is either analytic or contradictory; for the decision whether there exists a class of observation sentences which entail *S*, i.e., whether such observation sentences can be formulated, no matter whether they are true or false—that decision is a purely logical matter.

Incidentally, statements of the kind mentioned by Russell, which are not actually verifiable by any human being, were explicitly recognized as cognitively significant already by Schlick (1936) Part V, who argued that the impossibility of verifying them was "merely empirical." The characterization of verifiability with the help of the concept of observation sentence as suggested here might serve as a more explicit and rigorous statement of that conception.

are both observable characteristics, and that the former does not logically entail the latter. Then the sentence

(S1) All storks are red-legged

is neither analytic nor contradictory; and clearly, it is not deducible from a finite set of observation sentences. Hence, under the contemplated criterion, S1 is devoid of empirical significance; and so are all other sentences purporting to express universal regularities or general laws. And since sentences of this type constitute an integral part of scientific theories, the verifiability requirement must be regarded as overly restrictive in this respect.

Similarly, the criterion disqualifies all sentences such as 'For any substance there exists some solvent', which contain both universal and existential quantifiers (i.e., occurrences of the terms 'all' and 'some' or their equivalents); for no sentences of this kind can be logically deduced from any finite set of observation sentences.

Two further defects of the verifiability requirement do not seem to have been widely noticed:

b. As is readily seen, the negation of S1

(~S1) There exists at least one stork that is not red-legged

is deducible from any two observation sentences of the type 'a is a stork' and 'a is not red-legged'. Hence, ~S1 is cognitively significant under our criterion, but S1 is not, and this constitutes a violation of condition (A1).

c. Let *S* be a sentence which does, and *N* a sentence which does not satisfy the verifiability requirement. Then *S* is deducible from some set of observation sentences; hence, by a familiar rule of logic, *S*∨*N* is deducible from the same set, and therefore cognitively significant according to our criterion. This violates condition (A2) above.⁴

Strictly analogous considerations apply to an alternative criterion, which

4. The arguments here adduced against the verifiability criterion also prove the inadequacy of a view closely related to it, namely that two sentences have the same cognitive significance if any set of observation sentences which would verify one of them would also verify the other, and conversely. Thus, e.g., under this criterion, any two general laws would have to be assigned the same cognitive significance, for no general law is verified by any set of observation sentences. The view just referred to must be clearly distinguished from a position which Russell examines in his critical discussion of the positivistic meaning criterion. It is "the theory that two propositions whose verified consequences are identical have the same significance" (1948), p. 448. This view is untenable indeed, for what consequences of a statement have actually been verified at a given time is obviously a matter of historical accident which cannot possibly serve to establish identity of cognitive significance. But I am not aware that any logical empiricist ever subscribed to that "theory."

makes complete falsifiability in principle the defining characteristic of empirical significance. Let us formulate this criterion as follows:

(2.2) REQUIREMENT OF COMPLETE FALSIFIABILITY IN PRINCIPLE. A sentence has empirical meaning if and only if its negation is not analytic and follows logically from some finite logically consistent class of observation sentences.

This criterion qualifies a sentence as empirically meaningful if its negation satisfies the requirement of complete verifiability; as it is to be expected, it is therefore inadequate on similar grounds as the latter:

(a) It denies cognitive significance to purely existential hypotheses, such as 'There exists at least one unicorn', and all sentences whose formulation calls for mixed—i.e., universal and existential—quantification, such as 'For every compound there exists some solvent', for none of these can possibly be conclusively falsified by a finite number of observation sentences.

(b) If 'P' is an observation predicate, then the assertion that all things have the property P is qualified as significant, but its negation, being equivalent to a purely existential hypothesis, is disqualified [cf. (a)]. Hence, criterion (2.2) gives rise to the same dilemma as (2.1).

(c) If a sentence S is completely falsifiable whereas N is a sentence which is not, then their conjunction, S·N (i.e., the expression obtained by connecting the two sentences by the word 'and') is completely falsifiable; for if the negation of S is entailed by a class of observation sentences, then the negation of S·N is, *a fortiori*, entailed by the same class. Thus, the criterion allows empirical significance to many sentences which an adequate empiricist criterion should rule out, such as 'All swans are white and the absolute is perfect.'

In sum, then, interpretations of the testability criterion in terms of complete verifiability or of complete falsifiability are inadequate because they are overly restrictive in one direction and overly inclusive in another, and because both of them violate the fundamental requirement A.

Several attempts have been made to avoid these difficulties by construing the testability criterion as demanding merely a partial and possibly indirect confirmability of empirical hypotheses by observational evidence.

A formulation suggested by Ayer⁵ is characteristic of these attempts to set up a clear and sufficiently comprehensive criterion of confirmability. It states, in effect, that a sentence S has empirical import if from S in conjunction with suitable subsidiary hypotheses it is possible to derive observation sentences which are not derivable from the subsidiary hypotheses alone.

This condition is suggested by a closer consideration of the logical structure of

5. (1936, 1946), Chap. I. The case against the requirements of verifiability and of falsifiability, and in favor of a requirement of partial confirmability and disconfirmability, is very clearly presented also by Pap (1949), chapter 13.

scientific testing; but it is much too liberal as it stands. Indeed, as Ayer himself has pointed out in the second edition of his book, *Language, Truth, and Logic*,⁶ his criterion allows empirical import to any sentence whatever. Thus, e.g., if S is the sentence 'The absolute is perfect', it suffices to choose as a subsidiary hypothesis the sentence 'If the absolute is perfect then this apple is red' in order to make possible the deduction of the observation sentence 'This apple is red', which clearly does not follow from the subsidiary hypothesis alone.

To meet this objection, Ayer proposed a modified version of his testability criterion. In effect, the modification restricts the subsidiary hypotheses mentioned in the previous version to sentences which either are analytic or can independently be shown to be testable in the sense of the modified criterion.⁷

But it can readily be shown that this new criterion, like the requirement of complete falsifiability, allows empirical significance to any conjunction S·N, where S satisfies Ayer's criterion while N is a sentence such as 'The absolute is perfect', which is to be disqualified by that criterion. Indeed, whatever consequences can be deduced from S with the help of permissible subsidiary hypotheses can also be deduced from S·N by means of the same subsidiary hypotheses; and as Ayer's new criterion is formulated essentially in terms of the deductibility of a certain type of consequence from the given sentence, it countenances S·N together with S. Another difficulty has been pointed out by Church, who has shown⁸ that if there are any three observation sentences none of which alone entails any of the others, then it follows for any sentence S whatsoever that either it or its denial has empirical import according to Ayer's revised criterion.

All the criteria considered so far attempt to explicate the concept of empirical significance by specifying certain logical connections which must obtain between a significant sentence and suitable observation sentences. It seems now that this type of approach offers little hope for the attainment of precise criteria of meaningfulness: this conclusion is suggested by the preceding survey of some representative attempts, and it receives additional support from certain further considerations, some of which will be presented in the following sections.

3. CHARACTERIZATION OF SIGNIFICANT SENTENCES BY CRITERIA FOR THEIR CONSTITUENT TERMS

An alternative procedure suggests itself which again seems to reflect well

6. (1946), 2d ed., pp. 11-12.

7. This restriction is expressed in recursive form and involves no vicious circle. For the full statement of Ayer's criterion, see Ayer (1946), p. 13.

8. Church (1949). An alternative criterion recently suggested by O'Connor (1950) as a revision of Ayer's formulation is subject to a slight variant of Church's structure: It can be shown that if there are three observation sentences none of which entails any of the others, and if S is any noncompound sentence, then either S or \sim S is significant under O'Connor's criterion.

the general viewpoint of empiricism: It might be possible to characterize cognitively significant sentences by certain conditions which their constituent terms have to satisfy. Specifically, it would seem reasonable to say that all extralogical terms⁹ in a significant sentence must have experiential reference, and that therefore their meanings must be capable of explication by reference to observables exclusively.¹⁰ In order to exhibit certain analogies between this approach and the previous one, we adopt the following terminological conventions:

Any term that may occur in a cognitively significant sentence will be called a *cognitively significant term*. Furthermore, we shall understand by an *observation term* any term which either (a) is an *observation predicate*, i.e., signifies some observable characteristic (as do the terms 'blue', 'warm', 'soft', 'coincident with', 'of greater apparent brightness than') or (b) names some physical object of macroscopic size (as do the terms 'the needle of this instrument', 'the Moon', 'Krakatoa Volcano', 'Greenwich, England', 'Julius Caesar').

Now while the testability criteria of meaning aimed at characterizing the cognitively significant sentences by means of certain inferential connections in which they must stand to some observation sentences, the alternative approach under consideration would instead try to specify the vocabulary that may be used in forming significant sentences. This vocabulary, the class of significant terms, would be characterized by the condition that each of its elements is either a logical term or else a term with empirical significance; in the latter case, it has to stand in certain definitional or explicative connections to some observation terms. This approach certainly avoids any violations of our earlier conditions of adequacy. Thus, e.g., if *S* is a significant sentence, i.e., contains cognitively significant terms only, then so is its denial, since the denial sign, and its verbal equivalents, belong to the vocabulary of logic and are thus significant. Again, if *N* is a sentence containing a non-significant term, then so is any compound sentence which contains *N*.

But this is not sufficient, of course. Rather, we shall now have to consider a crucial question analogous to that raised by the previous approach: Precisely how are the logical connections between empirically significant terms and observation terms to be construed if an adequate criterion of cognitive significance is to result? Let us consider some possibilities.

9. An extralogical term is one that does not belong to the specific vocabulary of logic. The following phrases, and those definable by means of them, are typical examples of logical terms: 'not', 'or', 'if... then', 'all', 'some', '...', is an element of class...'. Whether it is possible to make a sharp theoretical distinction between logical and extra-logical terms is a controversial issue related to the problem of discriminating between analytic and synthetic sentences. For the purpose at hand, we may simply assume that the logical vocabulary is given by enumeration.

10. For a detailed exposition and critical discussion of this idea, see H. Feigl's stimulating and enlightening article (1950).

(3.1) The simplest criterion that suggests itself might be called the *requirement of definability*. It would demand that any term with empirical significance must be explicitly definable by means of observation terms.

This criterion would seem to accord well with the maxim of operationalism that all significant terms of empirical science must be introduced by operational definitions. However, the requirement of definability is vastly too restrictive, for many important terms of scientific and even pre-scientific discourse cannot be explicitly defined by means of observation terms.

In fact, as Carnap¹¹ has pointed out, an attempt to provide explicit definitions in terms of observables encounters serious difficulties as soon as disposition terms, such as 'soluble', 'malleable', 'electric conductor', etc., have to be accounted for; and many of these occur even on the pre-scientific level of discourse.

Consider, for example, the word 'fragile'. One might try to define it by saying that an object *x* is fragile if and only if it satisfies the following condition: If at any time *t* the object is sharply struck, then it breaks at that time. But if the statement connectives in this phrasing are construed truth-functionally, so that the definition can be symbolized by

$$(D) \quad Fx \equiv (t) [Sxt \supset Bxt]$$

then the predicate '*F*' thus defined does not have the intended meaning. For let *a* be any object which is not fragile (e.g., a raindrop or a rubber band), but which happens not to be sharply struck at any time throughout its existence. Then '*Sat*' is false and hence '*Sat* \supset *Bat*' is true for all values of '*t*'; consequently, '*Fa*' is true though *a* is not fragile.

To remedy this defect, one might construe the phrase 'if... then...' in the original definition as having a more restrictive meaning than the truth-functional conditional. This meaning might be suggested by the subjunctive phrasing 'If *x* were to be sharply struck at any time *t*, then *x* would break at *t*.' But a satisfactory elaboration of this construal would require a clarification of the meaning and the logic of counterfactual and subjunctive conditionals, which is a thorny problem.¹² An alternative procedure was suggested by Carnap in his theory of reduction sentences.¹³ These are sentences which, unlike definitions, specify the meaning of a term only conditionally or partially. The term 'fragile', for example, might be introduced by the following reduction sentence:

$$(R) \quad (x) (t) [Sxt \supset (Fx \equiv Bxt)]$$

11. Cf. (1936-37), especially section 7.

12. On this subject, see for example Langford (1941); Lewis (1946), pp. 210-30; Chisholm (1946); Goodman (1947); Reichenbach (1947); Chapter VIII, Hempel and Oppenheim (1948), Part III; Popper (1949); and especially Goodman's further analysis (1955).

13. Cf. Carnap, *loc. cit.* note 11. For a brief elementary presentation of the main idea, see Carnap (1938), Part III. The sentence *R* here formulated for the predicate '*F*' illustrates only the simplest type of reduction sentence, the so-called bilateral reduction sentence.

which specifies that if x is sharply struck at any time t , then x is fragile if and only if x breaks at t .

Our earlier difficulty is now avoided, for if a is a nonfragile object that is never sharply struck, then that expression in R which follows the quantifiers is true of a ; but this does not imply that ' Fa ' is true. But the reduction sentence R specifies the meaning of ' F ' only for application to those objects which meet the "test condition" of being sharply struck at some time; for these it states that fragility then amounts to breaking. For objects that fail to meet the test condition, the meaning of ' F ' is left undetermined. In this sense, reduction sentences have the character of partial or conditional definitions.

Reduction sentences provide a satisfactory interpretation of the experiential import of a large class of disposition terms and permit a more adequate formulation of so-called operational definitions, which, in general, are not complete definitions at all. These considerations suggest a greatly liberalized alternative to the requirement of definability:

(3.2) *The requirement of reducibility.* Every term with empirical significance must be capable of introduction, on the basis of observation terms, through chains of reduction sentences.

This requirement is characteristic of the liberalized versions of positivism and physicalism which, since about 1936, have superseded the older, overly narrow conception of a full definability of all terms of empirical science by means of observables,¹⁴ and it avoids many of the shortcomings of the latter. Yet, reduction sentences do not seem to offer an adequate means for the introduction of the central terms of advanced scientific theories, often referred to as theoretical constructs. This is indicated by the following considerations: A chain of reduction sentences provides a necessary and a sufficient condition for the applicability of the term it introduces. (When the two conditions coincide, the chain is tantamount to an explicit definition.) But now take, for example, the concept of length as used in classical physical theory. Here, the length in centimeters of the distance between two points may assume any positive real number as its value; yet it is clearly impossible to formulate, by means of observation terms, a sufficient condition for the applicability of such expressions as 'having a length of $\sqrt{2}$ cm' and 'having a length of $\sqrt{2} + 10^{-100}$ cm'; for such conditions would provide a possibility for discrimination, in observational terms, between two lengths which differ by only 10^{-100} cm.¹⁵

14. Cf. the analysis in Carnap (1936-37), especially section 15; also see the briefer presentation of the liberalized point of view in Carnap (1938).

15. (Added in 1964.) This is not strictly correct. For a more circumspect statement, see note 12 in "A Logical Appraisal of Operationalism" and the fuller discussion in section 7 of the essay "The Theoretician's Dilemma." Both of these pieces are reprinted in the present volume.

It would be ill-advised to argue that for this reason, we ought to permit only such values of the magnitude, length, as permit the statement of sufficient conditions in terms of observables. For this would rule out, among others, all irrational numbers and would prevent us from assigning, to the diagonal of a square with sides of length 1, the length $\sqrt{2}$, which is required by Euclidean geometry. Hence, the principles of Euclidean geometry would not be universally applicable in physics. Similarly, the principles of the calculus would become inapplicable, and the system of scientific theory as we know it today would be reduced to a clumsy, unmanageable torso. This, then, is no way of meeting the difficulty. Rather, we shall have to analyze more closely the function of constructs in scientific theories, with a view to obtaining through such an analysis a more adequate characterization of cognitively significant terms.

Theoretical constructs occur in the formulation of scientific theories. These may be conceived of, in their advanced stages, as being stated in the form of deductively developed axiomatized systems. Classical mechanics, or Euclidean or some Non-Euclidean form of geometry in physical interpretation, present examples of such systems. The extralogical terms used in a theory of this kind may be divided, in familiar manner, into primitive or basic terms, which are not defined within the theory, and defined terms, which are explicitly defined by means of the primitives. Thus, e.g., in Hilbert's axiomatization of Euclidean geometry, the terms 'point', 'straight line', 'between' are among the primitives, while 'line segment', 'angle', 'triangle', 'length' are among the defined terms. The basic and the defined terms together with the terms of logic constitute the vocabulary out of which all the sentences of the theory are constructed. The latter are divided, in an axiomatic presentation, into primitive statements (also called postulates or basic statements) which, in the theory, are not derived from any other statements, and derived ones, which are obtained by logical deduction from the primitive statements.

From its primitive terms and sentences, an axiomatized theory can be developed by means of purely formal principles of definition and deduction, without any consideration of the empirical significance of its extralogical terms. Indeed, this is the standard procedure employed in the axiomatic development of uninterpreted mathematical theories such as those of abstract groups or rings or lattices, or any form of pure (i.e., noninterpreted) geometry.

However, a deductively developed system of this sort can constitute a scientific theory only if it has received an empirical interpretation¹⁶ which

16. The interpretation of formal theories has been studied extensively by Reichenbach, especially in his pioneer analyses of space and time in classical and in relativistic physics. He describes such interpretation as the establishment of *coordinating definitions* (Zuordnungsdefinitionen) for certain terms of the formal theory. See, for example, Reichenbach (1928). More recently, (continued overleaf)

renders it relevant to the phenomena of our experience. Such interpretation is given by assigning a meaning, in terms of observables, to certain terms or sentences of the formalized theory. Frequently, an interpretation is given not for the primitive terms or statements but rather for some of the terms definable by means of the primitives, or for some of the sentences deducible from the postulates.¹⁷ Furthermore, interpretation may amount to only a partial assignment of meaning. Thus, e.g., the rules for the measurement of length by means of a standard rod may be considered as providing a *partial* empirical interpretation for the term 'the length, in centimeters, of interval i ', or alternatively, for some sentences of the form 'the length of interval i is r centimeters'. For the method is applicable only to intervals of a certain medium size, and even for the latter it does not constitute a full interpretation since the use of a standard rod does not constitute the only way of determining length: various alternative procedures are available involving the measurement of other magnitudes which are connected, by general laws, with the length that is to be determined.

This last observation, concerning the possibility of an indirect measurement of length by virtue of certain laws, suggests an important reminder. It is not correct to speak, as is often done, of "the experiential meaning" of a term or a sentence in isolation. In the language of science, and for similar reasons even in pre-scientific discourse, a single statement usually has no experiential implications. A single sentence in a scientific theory does not, as a rule, entail any observation sentences; consequences asserting the occurrence of certain observable phenomena can be derived from it only by conjoining it with a set of other, subsidiary, hypotheses. Of the latter, some will usually be observation sentences, others will be previously accepted theoretical statements. Thus, e.g., the relativistic theory of the deflection of light rays in the gravitational field of the sun entails assertions about observable phenomena only if it is conjoined with a considerable body of astronomical and optical theory as well as a large number of specific statements about the instruments used in those observations of solar eclipses which serve to test the hypothesis in question.

Hence, the phrase, 'the experiential meaning of expression E ' is elliptical. What

17. A somewhat fuller account of this type of interpretation may be found in Carnap (1939), §24. The articles by Spence (1944) and by MacCorquodale and Meehl (1948) provide enlightening illustrations of the use of theoretical constructs in a field outside that of the physical sciences, and of the difficulties encountered in an attempt to analyze in detail their function and interpretation.

Northrop [cf. (1947), Chap. VII, and also the detailed study of the use of deductively formalized theories in science, *ibid.*, Chaps. IV, V, VI] and H. Margenau [cf., for example, (1935)] have discussed certain aspects of this process under the title of *epistemic correlation*.

a given expression "means" in regard to potential empirical data is relative to two factors, namely:

- I. *the linguistic framework L* to which the expression belongs. Its rules determine, in particular, what sentences—observational or otherwise—may be inferred from a given statement or class of statements;
- II. the theoretical context in which the expression occurs, i.e., the class of those statements in L which are available as subsidiary hypotheses.

Thus, the sentence formulating Newton's law of gravitation has no experiential meaning by itself; but when used in a language whose logical apparatus permits the development of the calculus, and when combined with a suitable system of other hypotheses—including sentences which connect some of the theoretical terms with observation terms and thus establish a partial interpretation—then it has a bearing on observable phenomena in a large variety of fields. Analogous considerations are applicable to the term 'gravitational field', for example. It can be considered as having experiential meaning only within the context of a theory, which must be at least partially interpreted; and the experiential meaning of the term—as expressed, say, in the form of operational criteria for its application—will depend again on the theoretical system at hand, and on the logical characteristics of the language within which it is formulated.

4. COGNITIVE SIGNIFICANCE AS A CHARACTERISTIC OF INTERPRETED SYSTEMS

The preceding considerations point to the conclusion that a satisfactory criterion of cognitive significance cannot be reached through the second avenue of approach here considered, namely by means of specific requirements for the terms which make up significant sentences. This result accords with a general characteristic of scientific (and, in principle, even pre-scientific) theorizing: Theory formation and concept formation go hand in hand; neither can be carried on successfully in isolation from the other.

If, therefore, cognitive significance can be attributed to anything, then only to entire theoretical systems formulated in a language with a well-determined structure. And the decisive mark of cognitive significance in such a system appears to be the existence of an interpretation for it in terms of observables. Such an interpretation might be formulated, for example, by means of conditional or biconditional sentences connecting nonobservational terms of the system with observation terms in the given language; the latter as well as the connecting sentences may or may not belong to the theoretical system.

But the requirement of partial interpretation is extremely liberal; it is satisfied, for example, by the system consisting of contemporary physical theory combined with some set of principles of speculative metaphysics, even if the latter

have no empirical interpretation at all. Within the total system, these metaphysical principles play the role of what K. Reisch and also O. Neurath liked to call *isolated sentences*: They are neither purely formal truths or falsehoods, demonstrable or retriable by means of the logical rules of the given language system; nor do they have any experiential bearing; i.e., their omission from the theoretical system would have no effect on its explanatory and predictive power in regard to potentially observable phenomena (i.e., the kind of phenomena described by observation sentences). Should we not, therefore, require that a cognitively significant system contain no isolated sentences? The following criterion suggests itself:

(4.1) A theoretical system is cognitively significant if and only if it is partially interpreted to at least such an extent that none of its primitive sentences is isolated.

But this requirement may bar from a theoretical system certain sentences which might well be viewed as permissible and indeed desirable. By way of a simple illustration, let us assume that our theoretical system T contains the primitive sentence

$$(S1) \quad (x) [P_1x \supset (Qx \equiv P_2x)]$$

where ' P_1 ' and ' P_2 ' are observation predicates in the given language L , while ' Q ' functions in T somewhat in the manner of a theoretical construct and occurs in only one primitive sentence of T , namely $S1$. Now $S1$ is not a truth or falsehood of formal logic; and furthermore, if $S1$ is omitted from the set of primitive sentences of T , then the resulting system, T' , possesses exactly the same systematic, i.e., explanatory and predictive, power as T . Our contemplated criterion would therefore qualify $S1$ as an isolated sentence which has to be eliminated—excised by means of Occam's razor, as it were—if the theoretical system at hand is to be cognitively significant.

But it is possible to take a much more liberal view of $S1$ by treating it as a partial definition for the theoretical term ' Q '. Thus conceived, $S1$ specifies that in all cases where the observable characteristic P_1 is present, ' Q ' is applicable if and only if the observable characteristic P_2 is present as well. In fact, $S1$ is an instance of those partial, or conditional, definitions which Carnap calls bilateral reduction sentences. These sentences are explicitly qualified by Carnap as analytic (though not, of course, as truths of formal logic), essentially on the ground that all their consequences which are expressible by means of observation predicates (and logical terms) alone are truths of formal logic.¹⁸

Let us pursue this line of thought a little further. This will lead us to some observations on analytic sentences and then back to the question of the adequacy of (4.1).

18. Cf. Carnap (1936-37), especially sections 8 and 10.

Suppose that we add to our system T the further sentence

$$(S2) \quad (x) [P_3x \supset (Qx \equiv P_4x)]$$

where ' P_3 ', ' P_4 ' are additional observation predicates. Then, on the view that "every bilateral reduction sentence is analytic",¹⁹ $S2$ would be analytic as well as $S1$. Yet, the two sentences jointly entail non-analytic consequences which are expressible in terms of observation predicates alone, such as²⁰

$$(O) \quad (x) [\sim (P_1x \cdot P_2x \cdot P_3x \cdot \sim P_4x) \cdot \sim (P_1x \cdot \sim P_2x \cdot P_3x \cdot P_4x)]$$

But one would hardly want to admit the consequence that the conjunction of two analytic sentences may be synthetic. Hence if the concept of analyticity can be applied at all to the sentences of interpreted deductive systems, then it will have to be relativized with respect to the theoretical context at hand. Thus, e.g., $S1$ might be qualified as analytic relative to the system T , whose remaining postulates do not contain the term ' Q ', but as synthetic relative to the system T' enriched by $S2$. Strictly speaking, the concept of analyticity has to be relativized also in regard to the rules of the language at hand, for the latter determine what observational or other consequences are entailed by a given sentence. This need for at least a twofold relativization of the concept of analyticity was almost to be expected in view of those considerations which required the same twofold relativization for the concept of experiential meaning of a sentence.

If, on the other hand, we decide not to permit $S1$ in the role of a partial definition and instead reject it as an isolated sentence, then we are led to an analogous conclusion: Whether a sentence is isolated or not will depend on the linguistic frame and on the theoretical context at hand: While $S1$ is isolated relative to T (and the language in which both are formulated), it acquires definite experiential implications when T is enlarged by $S2$.

Thus we find, on the level of interpreted theoretical systems, a peculiar rapprochement, and partial fusion, of some of the problems pertaining to the concepts of cognitive significance and of analyticity: Both concepts need to be relativized; and a large class of sentences may be viewed, apparently with equal right, as analytic in a given context, or as isolated, or nonsignificant, in respect to it.

In addition to barring, as isolated in a given context, certain sentences which could just as well be construed as partial definitions, the criterion (4.1) has another serious defect. Of two logically equivalent formulations of a theoretical system it may qualify one as significant while barring the other as containing

19. Carnap (1936-37), p. 452.

20. The sentence O is what Carnap calls the *representative sentence* of the couple consisting of the sentences $S1$ and $S2$; see (1936-37), pp. 450-53.

an isolated sentence among its primitives. For assume that a certain theoretical system T_1 contains among its primitive sentences S', S'', \dots exactly one, S' , which is isolated. Then T_1 is not significant under (4.1). But now consider the theoretical system T_2 obtained from T_1 by replacing the two first primitive sentences, S', S'' , by one, namely their conjunction. Then, under our assumptions, none of the primitive sentences of T_2 is isolated, and T_2 , though equivalent to T_1 , is qualified as significant by (4.1). In order to do justice to the intent of (4.1), we would therefore have to lay down the following stricter requirement:

(4.2) A theoretical system is cognitively significant if and only if it is partially interpreted to such an extent that in no system equivalent to it at least one primitive sentence is isolated.

Let us apply this requirement to some theoretical system whose postulates include the two sentences S_1 and S_2 considered before, and whose other postulates do not contain 'Q' at all. Since the sentences S_1 and S_2 together entail the sentence O , the set consisting of S_1 and S_2 is logically equivalent to the set consisting of S_1 , S_2 and O . Hence, if we replace the former set by the latter, we obtain a theoretical system equivalent to the given one. In this new system, both S_1 and S_2 are isolated since, as can be shown, their removal does not affect the explanatory and predictive power of the system in reference to observable phenomena. To put it intuitively, the systematic power of S_1 and S_2 is the same as that of O . Hence, the original system is disqualified by (4.2). From the viewpoint of a strictly sensationalist positivism as perhaps envisaged by Mach, this result might be hailed as a sound repudiation of theories making reference to fictitious entities, and as a strict insistence on theories couched exclusively in terms of observables. But from a contemporary vantage point, we shall have to say that such a procedure overlooks or misjudges the important function of constructs in scientific theory: The history of scientific endeavor shows that if we wish to arrive at precise, comprehensive, and well-confirmed general laws, we have to rise above the level of direct observation. The phenomena directly accessible to our experience are not connected by general laws of great scope and rigor. Theoretical constructs are needed for the formulation of such higher-level laws. One of the most important functions of a well-chosen construct is its potential ability to serve as a constituent in ever new general connections that may be discovered; and to such connections we would blind ourselves if we insisted on banning from scientific theories all those terms and sentences which could be "dispensed with" in the sense indicated in (4.2). In following such a narrowly phenomenalist or positivistic course, we would deprive ourselves of the tremendous fertility of theoretical constructs, and we would often render the formal structure of the expurgated theory clumsy and inefficient.

Criterion (4.2), then, must be abandoned, and considerations such as those

outlined in this paper seem to lend strong support to the conjecture that no adequate alternative to it can be found; i.e., that it is not possible to formulate general and precise criteria which would separate those partially interpreted systems whose isolated sentences might be said to have a significant function from those in which the isolated sentences are, so to speak, mere useless appendages.

We concluded earlier that cognitive significance in the sense intended by recent empiricism and operationism can at best be attributed to sentences forming a theoretical system, and perhaps rather to such systems as wholes. Now, rather than try to replace (4.2) by some alternative, we will have to recognize further that cognitive significance in a system is a matter of degree: Significant systems range from those whose entire extralogical vocabulary consists of observation terms, through theories whose formulation relies heavily on theoretical constructs, on to systems with hardly any bearing on potential empirical findings. Instead of dichotomizing this array into significant and non-significant systems it would seem less arbitrary and more promising to appraise or compare different theoretical systems in regard to such characteristics as these:

- a. the clarity and precision with which the theories are formulated, and with which the logical relationships of their elements to each other and to expressions couched in observational terms have been made explicit;
- b. the systematic, i.e., explanatory and predictive, power of the systems in regard to observable phenomena;
- c. the formal simplicity of the theoretical system with which a certain systematic power is attained;
- d. the extent to which the theories have been confirmed by experimental evidence.

Many of the speculative philosophical approaches to cosmology, biology, or history, for example, would make a poor showing on practically all of these counts and would thus prove no matches to available rival theories, or would be recognized as so unpromising as not to warrant further study or development.

If the procedure here suggested is to be carried out in detail, so as to become applicable also in less obvious cases, then it will be necessary, of course, to develop general standards, and theories pertaining to them, for the appraisal and comparison of theoretical systems in the various respects just mentioned. To what extent this can be done with rigor and precision cannot well be judged in advance. In recent years, a considerable amount of work has been done towards a definition and theory of the concept of degree of confirmation, or logical probability, of a theoretical system,²¹ and several contributions have been made towards the

21. Cf., for example, Carnap (1945) and (1945)2, and especially (1950). Also see Helmer and Oppenheim (1945).

clarification of some of the other ideas referred to above.²² The continuation of this research represents a challenge for further constructive work in the logical and methodological analysis of scientific knowledge.

22. On simplicity, cf. especially Popper (1935), Chap. V; Reichenbach (1938), § 42; Goodman (1949)1, (1949)2, (1950); on explanatory and predictive power, cf. Hempel and Oppenheim (1948), Part IV.

REFERENCES

- Ayer, A. J., *Language, Truth and Logic*, London, 1936; 2nd ed. 1946.
- Carnap, R., "Testability and Meaning," *Philosophy of Science*, 3 (1936) and 4 (1937).
- Carnap, R., "Logical Foundations of the Unity of Science," in: *International Encyclopedia of Unified Science*, I, 1; Chicago, 1938.
- Carnap, R., *Foundations of Logic and Mathematics*, Chicago, 1939.
- Carnap, R., "On Inductive Logic," *Philosophy of Science*, 12 (1945). Referred to as (1945)1 in this article.
- Carnap, R., "The Two Concepts of Probability," *Philosophy and Phenomenological Research*, 5 (1945). Referred to as (1945)2 in this article.
- Carnap, R., *Logical Foundations of Probability*, Chicago, 1950.
- Chisholm, R. M., "The Contrary-to-Fact Conditional," *Mind*, 55 (1946).
- Church, A., Review of Ayer (1946), *The Journal of Symbolic Logic*, 14 (1949), 52-53.
- Feigl, H., "Existential Hypotheses: Realistic vs. Phenomenalistic Interpretations," *Philosophy of Science*, 17 (1950).
- Goodman, N., "The Problem of Counterfactual Conditionals," *The Journal of Philosophy*, 44 (1947).
- Goodman, N., "The Logical Simplicity of Predicates," *The Journal of Symbolic Logic*, 14 (1949). Referred to as (1949)1 in this article.
- Goodman, N., "Some Reflections on the Theory of Systems," *Philosophy and Phenomenological Research*, 9 (1949). Referred to as (1949)2 in this article.
- Goodman, N., "An Improvement in the Theory of Simplicity," *The Journal of Symbolic Logic*, 15 (1950).
- Goodman, N., *Fact, Fiction, and Forecast*, Cambridge, Massachusetts, 1955.
- Helmert, O. and P. Oppenheim, "A Syntactical Definition of Probability and of Degree of Confirmation," *The Journal of Symbolic Logic*, 10 (1945).
- Hempel, C. G. and P. Oppenheim, "Studies in the Logic of Explanation," *Philosophy of Science*, 15 (1948). (Reprinted in this volume.)
- Langford, C. H., Review in *The Journal of Symbolic Logic*, 6 (1941), 67-68.
- Lewis, C. I., *An Analysis of Knowledge and Valuation*, La Salle, Ill., 1946.
- MacCorquodale, K. and P. E. Meehl, "On a Distinction Between Hypothetical Constructs and Intervening Variables," *Psychological Review*, 55 (1948).
- Margenau, H., "Methodology of Modern Physics," *Philosophy of Science*, 2 (1935).
- Northrop, F. S. C., *The Logic of the Sciences and the Humanities*, New York, 1947.
- O'Connor, D. J., "Some Consequences of Professor A. J. Ayer's Verification Principle," *Analysis*, 10 (1950).
- Pap, A., *Elements of Analytic Philosophy*, New York, 1949.
- Popper, K., *Logik der Forschung*, Wien, 1935.
- Popper, K., "A Note on Natural Laws and So-Called 'Contrary-to-Fact Conditionals,'" *Mind*, 58 (1949).
- Reichenbach, H., *Philosophie der Raum-Zeit-Lehre*, Berlin, 1928.
- Reichenbach, H., *Elements of Symbolic Logic*, New York, 1947.
- Russell, B., *Human Knowledge*, New York, 1948.
- Schlick, M., "Meaning and Verification," *Philosophical Review*, 45 (1936). Also reprinted in Feigl, H. and W. Sellars, (eds.) *Readings in Philosophical Analysis*, New York, 1949.
- Spence, Kenneth W., "The Nature of Theory Construction in Contemporary Psychology," *Psychological Review*, 51 (1944).

COGNITIVE SIGNIFICANCE

The preceding essay is a conflation of two articles: "Problems and Changes in the Empiricist Criterion of Meaning," *Revue Internationale de Philosophie* No. 11 (1950), and "The Concept of Cognitive Significance: A Reconsideration," *Proceedings of the American Academy of Arts and Sciences* 80 (1951). In combining the two, I omitted particularly some parts of the first article, which had been largely superseded by the second one;¹ I also made a few minor changes in the remaining text. Some of the general problems raised in the combined essay are pursued further elsewhere in this volume, especially in "The Theoretician's Dilemma." In this Postscript, I propose simply to note some second thoughts concerning particular points in the preceding essay.

(i) The objections 2.1(c) and 2.2(c) against the requirements of complete verifiability and of complete falsifiability are, I think, of questionable force. For $S \vee N$ can properly be said to be entailed by S , and S in turn by $S \cdot N$, only if N as well as S is a declarative sentence and thus is either true or false. But if the criterion of cognitive significance is understood to delimit the class of sentences which make significant assertions, and which are thus either true or false, then the sentence N invoked in the objections is not declarative, and neither are $S \vee N$ or $S \cdot N$; hence the alleged inferences from $S \cdot N$ to S and from S to $S \vee N$ are inadmissible.²

1. The basic ideas presented in the earlier articles and in the present conflated version are penetratingly examined by I. Scheffler in *The Anatomy of Inquiry*, New York, 1963. Part II of his book deals in detail with the concept of cognitive significance.

2. I owe this correction to graduate students who put forth the above criticism in one of my seminars. The same point has recently been stated very clearly by D. Rynin in "Vindicacion de $FL * G * C * L * P * S * T * V * S * M$ ", *Proceedings and Addresses of the American Philosophical Association*, 30 (1957); see especially pp. 57-58.

My objection retains its force, however, against the use of falsifiability, not as a criterion of significance, but as a "criterion of demarcation." This use would draw a dividing line "between the statements, or systems of statements, of the empirical sciences, and all other statements—whether they are of a religious or of a metaphysical character, or simply pseudo-scientific."³ For the argument 2.2(c) shows that the conjunction of a scientific statement S with a nonscientific statement N is falsifiable and thus qualifies as a scientific statement; and this would defeat the intended purpose of the criterion of demarcation.

(ii) My assertion, in 2.1(a) and 2.2(a), that the requirements of verifiability and of falsifiability would rule out *all* hypotheses of mixed quantificational form is false. Consider the hypothesis 'All ravens are black and something is white', or, in symbolic notation

$$(x)(Rx \supset Bx) \cdot (\exists y) Wy,$$

which is equivalent to

$$(x)(\exists y)[(Rx \supset Bx) \cdot Wy]$$

This sentence satisfies the falsifiability requirement because it implies the purely universal hypothesis ' $(x)(Rx \supset Bx)$ ', which would be falsified, for example, by the following set of observation sentences: $\{Ra, \sim Ba\}$. Similarly, the sentence

$$(\exists x)(y)(Rx \vee Wy)$$

is verifiable since it is implied, for example, by ' Ra '.

The essential point of the objection remains unaffected, however: Many scientific hypotheses of mixed quantificational form are neither verifiable nor falsifiable; these would therefore be disqualified by the requirement of verifiability as well as by that of falsifiability; and if the latter is used as a criterion of demarcation rather than of significance, it excludes those hypotheses from the class of scientific statements. These consequences are unacceptable.

(iii) An even stronger criticism of the criteria of verifiability and of falsifiability results from condition (A1), which is stated early in section 2, and which demands in effect that any acceptable criterion of significance which admits a sentence as significant must also admit its negation. That this condition must be met is clear, for since a significant sentence is one that is either true or false, its negation can be held nonsignificant only on pain of violating a fundamental principle of logic. And even if the falsifiability criterion is used as a criterion of demarcation rather than of cognitive significance, satisfaction of (A1) seems imperative. Otherwise, a scientist reporting that he had succeeded in refuting a scientific hypothesis S of universal form would be making a nonscientific

3. K. R. Popper, "Philosophy of Science: A Personal Report," In C. A. Mace, ed., *British Philosophy in the Mid-Century*, London, 1957; pp. 155-91; quotations from pp. 163, 162.

statement if he were to say: "Hence, it is not the case that S holds," for this statement would not be falsifiable. More generally, formally valid deductive logical inference would often lead from scientific premises to nonscientific conclusions—e.g., from ' $Ra \sim Ba$ ' to ' $(\exists x)(Rx \sim Bx)$ '; and, surely, this is intolerable.

But when the requirement of verifiability, or that of falsifiability, is combined with condition (A1), then a sentence qualifies as cognitively significant just in case it and its negation are verifiable, or just in case it and its negation are falsifiable. These two criteria now demand the same thing of a significant sentence, namely, that it be both verifiable and falsifiable. This characterization admits, besides all truth-functional compounds of observation sentences, also certain sentences containing quantifiers. For example, ' $\forall x(x)Qx$ ' is verifiable by ' Pa ' and falsifiable by ' $\sim Pa$ '; ' $\sim Qb$ '; and as is readily seen, ' $Pa \cdot (\exists x)Qx$ ' equally meets the combined requirement. But this requirement excludes all strictly general hypotheses, i.e., those containing essential occurrences of quantifiers but not of individual constants; such as ' $(x)(Rx \supset Bx)$ ', ' $(x)(\exists y)(Rxy \supset Sxy)$ ', and so forth. Again, this consequence is surely unacceptable, no matter whether the criterion is meant to delimit the class of significant sentences or the class of statements of empirical science.

5. A LOGICAL APPRAISAL

OF OPERATIONISM

1. BASIC TENETS OF OPERATIONISM

OPERATIONISM, in its fundamental tenets, is closely akin to logical empiricism. Both schools of thought have put much emphasis on definite experiential meaning or import as a necessary condition of objectively significant discourse, and both have made strong efforts to establish explicit criteria of experiential significance. But logical empiricism has treated experiential import as a characteristic of statements—namely, as their susceptibility to test by experiment or observation—whereas operationism has tended to construe experiential meaning as a characteristic of concepts or of the terms representing them—namely, as their susceptibility to operational definition.

BASIC IDEAS OF OPERATIONAL ANALYSIS. An operational definition of a term is conceived as a rule to the effect that the term is to apply to a particular case if the performance of specified operations in that case yields a certain characteristic result. For example, the term 'harder than' might be operationally defined by the rule that a piece of mineral, x , is to be called harder than another piece of mineral, y , if the operation of drawing a sharp point of x across the surface of y results in a scratch mark on the latter. Similarly, the different numerical values of a quantity such as length are thought of as operationally definable by reference to the outcomes of specified measuring operations. To safeguard the objectivity of science, all operations invoked in this kind of definition are

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